

Role of structures on thermal conductivity in thermoelectric materials

C. Godart ¹, A.P. Gonçalves ², E.B. Lopes ², B. Villeroy ¹

³CNRS, ICMPE, CMTR, 2/8 rue Henri Dunant, 94320 Thiais, France

²Dep. Química, Instituto Tecnológico e Nuclear/CFMC-UL, P-2686-953 Sacavém, Portugal

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List of symbols:

α : Seebeck coefficient
 λ : thermal conductivity
 λ_e : electronic part of the thermal conductivity
 λ_L : phonon (lattice) part of the thermal conductivity
 μ : mobility
 ρ : electrical resistivity
 σ : electrical conductivity
 τ : Thomson coefficient
 Π : Peltier coefficient
ADP: Atomic Displacement Parameter
I: intensity
PGEC: Phonon Glass Electron Crystal
q: charge of a carrier
Q: heat quantity
S: entropy
TE: thermoelectric
V: potential
VEC: Valence Electron Concentration
ZT: Figure of merit

Abstract The figure of merit $ZT = \sigma\alpha^2T/\lambda$ (α the Seebeck coefficient, σ and λ the electrical and thermal conductivity, respectively) is an essential element of the efficiency of a thermoelectric material for applications, which convert heat to electricity or, conversely, electric current to cooling. From the expression of the power factor, $\sigma\alpha^2$, it was deduced that a highly degenerated semiconductor is necessary. In order to reduce the lattice part of the thermal conductivity, various mechanisms, mainly related to the structure of the materials, were tested in new thermoelectric materials and had been the topics of different reviews. These include cage-like materials, effects of vacancies, solid solutions, complex structures (cluster, tunnel, ...), nano-structured systems. We plan to review structural aspects in the modern thermoelectric materials and include results of the very last years in such view. Moreover, as micro- and nano-composites seem to be promising to increase ZT in large size samples, we will also briefly discuss the interest of spark plasma sintering technique to preserve the micro- or nano- structure in highly densified samples.

1. Introduction

Thermoelectric (TE) effects include the transformation of caloric energy to electric energy or its reverse, and their applications consequently include the two aspects: (micro)cooling or electricity generation from heat sources. Search for new friendly environmental energy sources recently became of major importance in our modern societies, specially after the signature of the Kyoto protocol. Consequently, the electricity generation from waste heat via thermoelectric modules (see Seebeck effect) can be seen as a new "green" energy source. Moreover, thermoelectric materials can be used to extract heat (see Peltier effect) from micro-electronic components. In the first case, the low efficiency of the thermoelectric systems has prevented their use during many years, but the situation is changing with increase of the needs (and cost) of energy and improved materials. In the latter case, classical methods (air/water) are no more appropriate due to miniaturization and high local power to dissipate. In both cases, new concepts lead, from ~1995, to rather remarkable progress, as well as the appearance of the topics in many conferences and national research programs in various countries.

The understanding of physical phenomena involved in thermoelectricity and the development of conventional TE materials occur during two main active period. From 1821 to 1851, the 3 TE effects (Seebeck, Peltier and Thomson) have been discovered and understood from a macroscopic point of view. Their potential for applications to temperature measurements, cooling and electricity production have also been established. Later on, from 1930 to the beginning of the sixties of the previous century, important progress occur both in the understanding of phenomena at a microscopic scale and in the discovery and optimization of presently used TE materials. However, the efficiency was not sufficient to compete with the cooling by compression/détente cycles or for economically profitable electricity production.

More recently, from the beginning of 1990's, a renewal of interest in TE appears, due to environmental concern with refrigerant gas and greenhouse effects, as well as the need to develop alternative energy sources.

The two main research directions happen to be - the development of new materials with complex or open structures, and - the development of already known materials under new low dimensionality forms (quantum wells, nano-wires, nanograins, thin films, nano-composites, ..). Among new materials having interesting TE characteristics for electricity generation from heat sources in the range 200-800°C we will emphasize the role of the structure and the potential of micro- and nano-structures to exceed the 14% efficiency reported by [Caillat 2004].

2. The thermoelectric effects

The first thermoelectric effect has been discovered by [Seebeck 1822] and understood later by Oersted: a potential appears at the junction of two materials a, b submitted to a gradient of temperature. The well known application of the Seebeck effect is the measurement of temperature by thermocouple. The Seebeck coefficient, $\alpha_{ab} = \Delta V / \Delta T$, is the entropy S per charge carrier q divided by the charge: $\alpha = S/q$. Later on, [Peltier 1834] has discovered the second effect: a temperature difference appears when a current I pass through the junctions of two different materials. There is absorption of heat Q at one junction and liberation of Q at the other junction, the Peltier coefficient is defined by $\Pi_{ab} = Q/I$. The third effect [Thomson 1851] occurs when both a gradient of temperature and an electric current exists simultaneously. When a current passes through a material submitted to a gradient of temperature, then the material exchanges heat with the outside medium. Conversely, a current is produced when a heat flux passes through a material submitted to a temperature gradient. The thermal flux, dQ/dx , is given by $\tau \cdot I \cdot dT/dx$ with τ the Thomson coefficient. The Peltier and Seebeck coefficients are related by : $\Pi = \alpha T = Q/I$.

3. Efficiencies, Figure of merit

For both cooling or generation, a TE module is made of couples n,p electrically connected. Each couple includes a p-type material ($\alpha > 0$) and a n-type material ($\alpha < 0$) in which charge carriers are holes and electrons, respectively. These two materials are joined by a conducting material assumed to be with $\alpha = 0$.

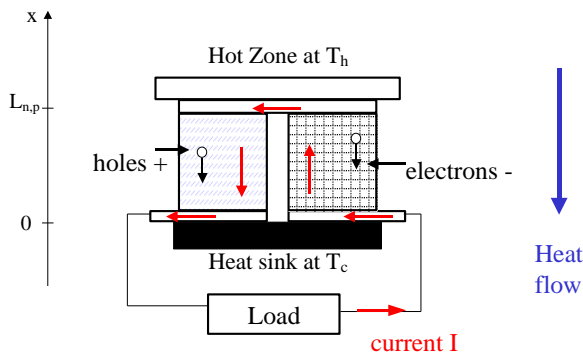


Fig. 3.1. Scheme of a TE couple for generation.

The two branches of the couple and all other couples of the module are connected electrically in series and thermally in parallel. The scheme of principle of a couple for generation is shown in Fig. 3.1. In the case of cooling, the load is replaced by a dc-current source, which oblige the charge carriers to move from the cold zone to the hot zone in both branches. This implies a thermal flux opposite to the normal heat conduction.

The optimization of the materials needs to optimize their transport properties in order to maximize the so-called figure of merit:

$$ZT = \sigma \alpha^2 T / \lambda \quad 1$$

with $\sigma = 1/\rho$ and λ the electrical and thermal conductivities, respectively.

For cooling applications, the efficiency of the system is given by the coefficient of performance COP which, in an optimized system, is:

$$COP = \frac{\gamma T_f - T_c}{(T_f - T_c)(1 + \gamma)} \quad 2$$

with $\gamma = \sqrt{1 + ZT}$, T_h and T_c the hot and cold temperatures respectively. For electricity generation, the maximum conversion efficiency is given by:

$$\eta_{\max} = \frac{(T_c - T_f)(\gamma - 1)}{T_f + \gamma T_c} \quad 3$$

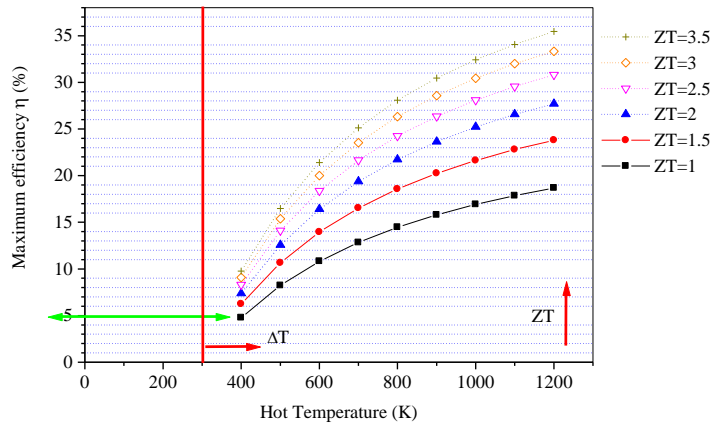


Fig. 3.2. Maximum efficiency for generation

From this expression, it is possible to estimate the maximum efficiency which can be expected for the couple versus the hot temperature (the cold one is taken as 300K) with different values of ZT (Fig. 3.2).

The green double arrow shows that for a $ZT=1$ and a temperature gradient of 100° , the efficiency is no more than 5%. To increase it, it is necessary to increase ZT or to increase the temperature gradient: in both cases, this leads to a problem of materials: 1- to increase ZT ; 2- to find materials stable at higher temperature.

In fact, the previous simple calculations assume that ZT is constant versus temperature, which is not correct specially if the temperature gradient is large (see below the curves of ZT for n- and p-type materials).

The expression of the figure of merit clearly sums up the difficulty to optimize the materials. Intuitively, it seems difficult for a material to simultaneously possesses a good electrical conductivity, characteristic of metals, and a bad thermal conductivity, characteristic of insulator. Closer examination of the power factor $\sigma\alpha^2$ [Gonçalves et al., in this volume] leads to consider semiconductors with a small gap and a carrier concentration in the range $[10^{18}-10^{21} \text{ cm}^{-3}]$. The second parameter is the thermal conductivity which, in such semiconductors, must be reduced.

4. Thermal conductivity, phonons

Intuitively, a good thermal conductivity would prevent to establish a large temperature gradient. However, the thermal conductivity includes mainly two components: an electronic contribution λ_e , due to the movement of carriers, and a lattice contribution via the phonons λ_L : $\lambda = \lambda_e + \lambda_L$. The electronic part of the thermal conductivity is related to the electronic conductivity via the Wiedemann-Franz law:

$$\lambda_e = L_0 T \sigma, \quad (4)$$

with L_0 the Lorentz factor. In metals, it is equal to the Lorentz number:

$$L_0 = \frac{\pi^2}{3} \left(\frac{k}{e} \right)^2 = 2,45 \cdot 10^{-8} \text{ V}^2 \cdot \text{K}^{-2}, \text{ value generally used as a first approximation}$$

for the TE semiconductors. Replacing λ by its two components and with the Wiedemann-Franz, leads to:

$$ZT = \frac{S^2 T \sigma}{L T \sigma + \lambda_L} \quad \text{or} \quad ZT = \frac{S^2}{L} \frac{\lambda_e}{\lambda_e + \lambda_L}. \quad (5)$$

This last expression shows that the optimization of ZT implies the minimization of the phonons contribution to λ . Assuming a negligible lattice contribution, from $ZT = \alpha^2 / L$, a ZT of 1 or 3¹ would be obtained from a Seebeck coefficient of 156 $\mu\text{V/K}$ or 270 $\mu\text{V/K}$, respectively. However, the minimization should not modify the electrical conductivity (as ZT increases with λ_e / λ_L). This leads to the proposition of [Slack 1995] to check materials which conducts electricity as a crystal and

¹ $ZT=3$ correspond to a COP of refrigeration of 1.1, typical of a compression fridge

heat as a glass, so-called "Phonon Glass Electron Crystal" (PGEC). This implies to find selective diffusion process which affects more the phonons than the carriers. Various physical process inducing significant phonon diffusion have been tested on TE materials, let us quote those that are somehow related with the structure:

- a complex crystalline structure will increase the number of optical phonon modes, whereas the heat is mainly conducted by acoustic phonons;

- the insertion of heavy atoms in empty cages of crystalline structure may let them rattle independently of the lattice and so, create new phonon modes (weakly dispersive optical modes);

- solid solutions between different materials with the same structure increase the disorder and create an important phonon diffusion by mass fluctuations on the sites [Abeles 1963], such mass fluctuations can also be obtained by vacancy creation in the material;

- impurities and point defects will diffuse phonons [Callaway 1960], [Klemens 1960], [Worlock 1966]: this leads to study micro- or nano-composites materials (mixing of a good TE material with another neutral for TE), or use "exotic" synthesis or shaping techniques inducing large amount of such defects,

- grain boundaries will affect phonons (and also electrical conductivity), this leads to study nano-crystalline materials to increase the number of such boundaries or even to reduce the mean free path of phonons (when the sizes of the nano-grains are comparable with that of the mean free path of phonons).

That different processes are not exclusives and some of them can be created simultaneously in the same TE material; some examples are given in the chapter by [Gonçalves et al., in this volume].

5. Conventional TE materials

From 1960, all actually used TE materials (see Table 5.1) were known and their performance, bound to a stagnant ZT to ~ 1 , have not much changed up to 1990.

The main market applications, were based on Bi_2Te_3 - type of material mainly used for cooling. Let us remark that no material was efficient in the temperature range 400-700K. At higher temperature, PbTe and TAGS (Te-Ag-Ge-Sb) have ZT ~ 1 in n- and p- type respectively.

	Bi-Sb	Bi ₂ Te ₃ -Sb ₂ Te ₃	(Bi,Sb) ₂ (Te,Sb) ₃	-	PbTe	Te-Ag-Ge-Sb	Si-Ge
Type	n	n,p	n,p	-	n	p	n,p
T _u (K)	200	<300	~300-400	-	700	750	1000
ZT at T _u	1.1 (H)	0.8	0.9	-	0.8	1.1	0.6

Table 5.1. ZT of conventional materials at their optimal temperature of use T_u (H means a value obtained under a magnetic field)

6. Recent bulk TE materials

6.1. ADP (Atomic Displacement Parameter)

In solids, the atoms don't move only at zero temperature. At finite temperature, the atoms vibrate around their equilibrium position on their crystallographic site, the mean square displacement amplitude of such atoms is called the Atomic Displacement Parameter, ADP, which is useful to estimate the minimum value of the lattice contribution to the thermal conductivity and is thus of interest in TE materials.

The vibrations of the atoms are generally non isotropic and this anisotropy is taken into account by a tensor of the ADP, noted U_{ij} . These U_{ij} are described by the ellipsoids of vibrations centered on each atom with an extension in one direction corresponding to the amplitude of the vibration in that direction. An isotropic ADP U_{iso} can be defined for each site, which is the mean value of the U_{ij} in all the directions of the space. Its amplitude allows to compare the overall movements of the different atoms of the structure. Generally the U_{iso} tends toward zero at zero temperature, and if not, this may indicate some static disorder on the site.

The minimal value of the lattice part of the thermal conductivity is given by $\lambda_L = (1/3)C_v v_s d$, with v_s the sound speed, d the mean free path of phonons and C_v the specific heat estimated from the Dulong and Petit law

$$C \xrightarrow{T \rightarrow \infty} 3R = 3N_A k_B \quad 6$$

(with R the constant of gas, N_A the Avogadro number). In the case of a cage like material, like LaB₆, (Fig. 6.1), the specific heat has been calculated from ADP of La and B atoms.

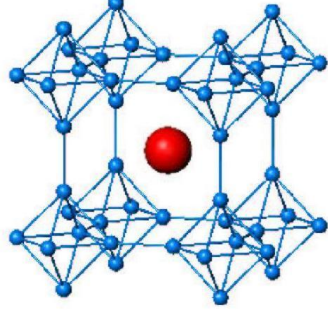


Fig. 6.1. Cage like structure of LaB_6 , the La atom \bullet is surrounded by B \bullet groups.

The La atom is considered as an Einstein oscillator in a solid of Debye of B-atoms. $C_V = fC_D + (1-f)C_E$ with f the fraction of atoms contributing to the solid of Debye and $(1-f)$ that of Einstein oscillators; θ_D and θ_E , the Debye and Einstein temperatures respectively:

$$C_D = 9N_A k_B \left(\frac{T}{\theta_D}\right)^3 \int_0^{\theta_D/T} \frac{x^4 e^x}{(e^x - 1)^2} dx \quad 7$$

and

$$C_E = 3N_A k_B \left(\frac{\theta_E}{T}\right)^2 \frac{e^{\theta_E/T}}{(1 - e^{\theta_E/T})^2} \quad 8$$

6.2. Cage like TE materials

Cage like TE materials have a rigid sub-lattice responsible for the electrical conductivity and large empty cages. When the cages are filled with heavy atoms, these atoms, weakly bound to the cage, can vibrate inside with a strong amplitude of vibrations. Initially it has been proposed that these vibrations are incoherent ("rattling") and act as traps for the acoustic phonons and consequently decrease the thermal conductivity. According to more recent work, the vibrations of the inserted atom are optical phonons (coherent vibrations) mainly without dispersion (localized character) and with a weak energy which strongly interfere with acoustic phonons to decrease the thermal conductivity.

The two most studied families of cage like TE materials are the filled skutterudites $A_y M_4 X_{12}$ (A: an electropositive element, M a metal and X=P, As, Sb) and the clathrates of the type $A_8 Y_{16} X_{30}$ (X and Y being actually mainly Ga and Ge), both of them leading to increased values of ZT.

6.2.a. Skutterudites

In the skutterudite, the atom A fills the cubic structure (space group $Im\bar{3}$) of the binary CoX_3 , which leads to the ternary filled structure $A_yM_4X_{12}$ [Jeitschko 1977] (Fig. 6.2).

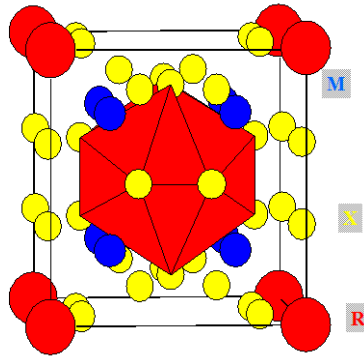


Fig. 6.2. Structure of filled skutterudite $A_yM_4X_{12}$

Atoms of various oxidation numbers (single valence K, Na; divalent Ca, Sr, Ba, trivalent La, Ce, Pr, Nd, Th, U; mixed valent Yb [Bérardan 2003]) can fill the cage with an occupation rate which depends on the nature of A (~ 1 with K and Na [Leithe Jasper 2003], but smaller with rare earths) and strongly on the nature of M (~ 0.2 with Co and ~ 0.9 with Fe) in rare earth based series (Table 6.1).

A= Ba	La	Ce	Eu	Yb	Tl
0.44	0.23	0.1	0.54	0.25	0.22
[Chen 2001]	[Nolas 1998]	[Chen 1997]	[Berger 2001]	[Anno 2000]	[Sales 2000]

Table 6.1. Occupation limits of A in $A_yCo_4Sb_{12}$

The cage in $CeFe_4Sb_{12}$ is well evidenced when looking on the distances between atoms (Fig. 6.3). The distance d (Ce-Sb)=3.39 Å, and the covalent radius R of Sb ($1/2 d(Sb-Sb)=1.46$ Å) gives $d-R=1.93$ Å \gg ionic radius of Ce = 1.14 Å.

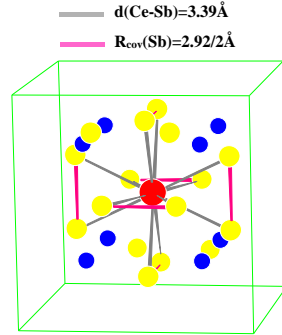


Fig. 6.3. Distances and cage in $\text{CeFe}_4\text{Sb}_{12}$

Consequently, two effects can affect λ_L : a strong vibration of A, seen by neutron diffraction [Sales 1997][Chakoumakos 1999] (Fig. 6.4), and a variable vacancy concentration rate in $\text{A}_y(\text{Fe,Co})_4\text{Sb}_{12}$.

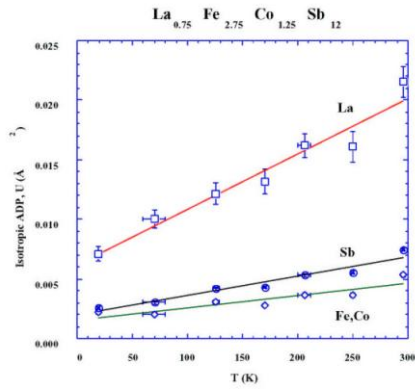


Fig. 6.4. Isotropic ADP in $\text{La}_y(\text{Fe,Co})_4\text{Sb}_{12}$.

As can be seen in Fig. 6.4, the ADP of La in $\text{La}_y(\text{Fe,Co})_4\text{Sb}_{12}$ is much higher than that of M and Sb atoms. The thermal conductivity is strongly reduced in the ternaries as compared to binaries. The smallest λ_L appears in antimonides, i.e., when the cage is larger (due to increase lattice parameter) and consequently when the amplitude of vibration is stronger (Fig. 6.5) [Fleurial 1997].

In the phenomenological model of [Sales 1999], [Sales 2000] for skutterudites, the filler atom is treated as an Einstein oscillator and the (M,X) lattice as a solid of Debye.

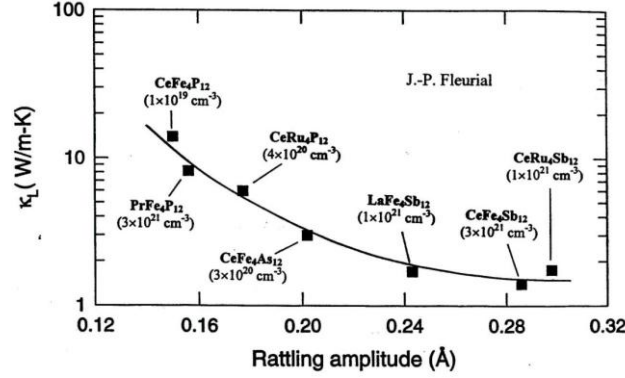


Fig. 6.5. Thermal conductivity versus the amplitude of rattling.

Samples	Type	highest ZT	T _{ZT} (K)	Ref.
B (CoSb ₃) _{0.75} +(FeSb ₂) _{0.25}	n	0.37	773	[Katsuyama 2000]
B Co _{0.94} Ni _{0.04} Sb ₃	n	0.5	750	[Katsuyama 2003]
B CoSb ₃	p	0.21	600	[Katsuyama 1998]
B CoSb ₃ + 0.75%Te	n	0.5	600	[Wojciechowski 2001]
B CoSb ₃ +4%Te	n	0.8	750	[Nagamoto 1998]
B IrSb ₃	p	0.15	800	[Slack 1994]
T Ba _{0.24} Co ₄ Sb _{11.87}	n	1.1	850	[Chen 2001]
T Ba _{0.3} Co _{3.95} Ni _{0.05} Sb ₁₂	n	1.2	800	[Dyck 2002]
T Ca _y Co _{4-x} Ni _x Sb ₁₂	p	1	800	[Puyet 2005]
T Ce _{0.28} Co _{2.5} Fe _{1.5} Sb ₁₂	p	1.1	800	[Tang 2001]
T Ce _x Fe _{3.5} Co _{0.5} Sb ₁₂	p	1.4 (1.2) ²	870	[Fleurial 1996]
T Eu _{0.42} Co ₄ Sb _{11.37} Ge _{0.50}	n	1.1	700	[Lamberton 2002]
T In _{0.25} Co ₄ Sb ₁₂	n	1.2	570	[He 2006]
T In _{0.2} Ce _{0.2} Co ₄ Sb ₁₂	n	1.7	570	[He 2005]
T La _x Fe _{4-y} Co _y Sb ₁₂	p	1	800	[Sales 1996]
T Nd _x Co ₄ Sb ₁₂	n	0.45	700	[Kuznetsov 2003]
T Ti _x Co ₄ Sb ₁₂	n	0.2	300	[Sales 2000]
T Yb _{0.8} Fe _{3.4} Ni _{0.6} Sb ₁₂	p	1	800	[Anno 2002]
T Yb _{0.19} Co ₄ Sb ₁₂	n	>1	600	[Nolas 2000]
T (Ce,Yb) _{0.4} Fe ₃ CoSb ₁₂	p	1	800	[Bérardan 2005]

Table 6.2. Highest ZT in binary (B) and ternary (T) skutterudites

² calculated values of 1.2 from experimental data

By appropriate substitutions, keeping the semiconducting (semi-metallic) state, the values of ZT have been strongly improved from a maximum value of ~ 0.8 (Table 6.2) in CoSb_3 to higher than 1 in various series, with both n- and p- type (Table 6.2).

Let us note that the possibility to obtain both types, with high ZT, in the same temperature range, with chemically rather similar materials is a positive point of these series, as similar behaviors is expected when used in applications.

6.2.b Clathrates $\text{A}_8\text{Ga}_{16}\text{Ge}_{30}$ (A=Ba, Eu, Sr)

Clathrates are compounds made by inclusion of molecules of one species in cavity of a crystalline lattice of another species: they consequently are cage like compounds. In this article we are only concerned with semiconducting clathrates. The family of clathrates [Kaspar 1965], derived from the binary A_8X_{46} (A= alkaline or alkaline earth, X= Si, Ge), comprise numerous structures built from complex polyhedron of X elements (X_{20} , X_{24} , ..) filled by the electropositive element A (Fig. 6.6).

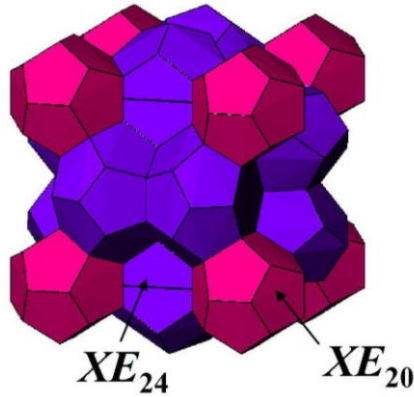


Fig. 6.6. The 2 types of polyhedron X_{20} and X_{24} around A atom in the type I clathrate $\text{A}_8\text{Ga}_{16}\text{Ge}_{30}$.

The type I structure, made from 2 polyhedron X_{20} and 6X_{24} , leads to a metallic character; a semiconducting state is obtained by substituting X by an element which accepts the electrons from A-metal. If A is divalent this means to replace 16 Ge (Si) by 16 Ga which leads to $\text{A}^{2+}_8\text{Ga}^{16}_-\text{Ge}^{30}_0$ (cubic, space group $\text{Pm}\bar{3}\text{n}$). In the cage X_{24} , the inserted atom has strong vibration amplitudes (Fig. 6.7) [Chakoumakos 2000]

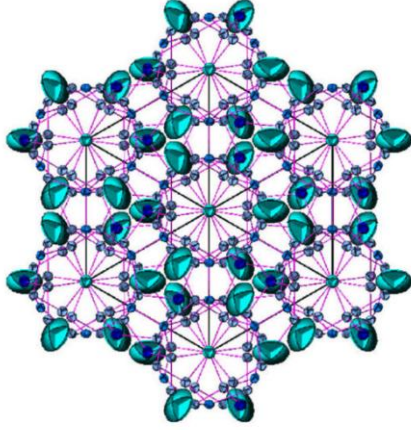


Fig. 6.7. View, along 111 projection, of the ellipsoids of movement of Sr in $\text{Sr}_8\text{Ga}_{16}\text{Ge}_{30}$.

Consequently, the ADP values on the site Sr2 are higher than that on site Sr1 (Fig. 6.8), the strong residual component at low temperature being due to static disorder on this site. The filling of the cages induces strong decreases of the thermal conductivity which becomes as low as in glass or quartz [Nolas 1998].

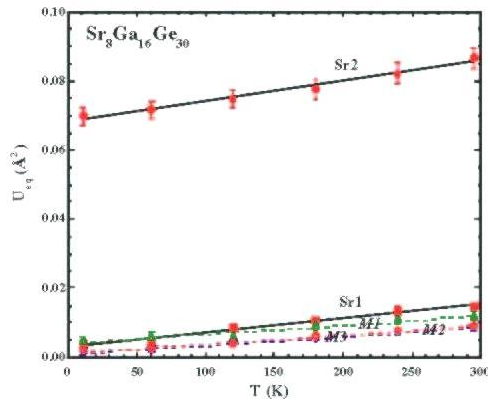


Fig. 6.8. Values of ADP for the different sites in $\text{Sr}_8\text{Ga}_{16}\text{Ge}_{30}$.

Presently, the type I has lead to ZT values highest than 1 [Anno 2002],[Bentien 2003].

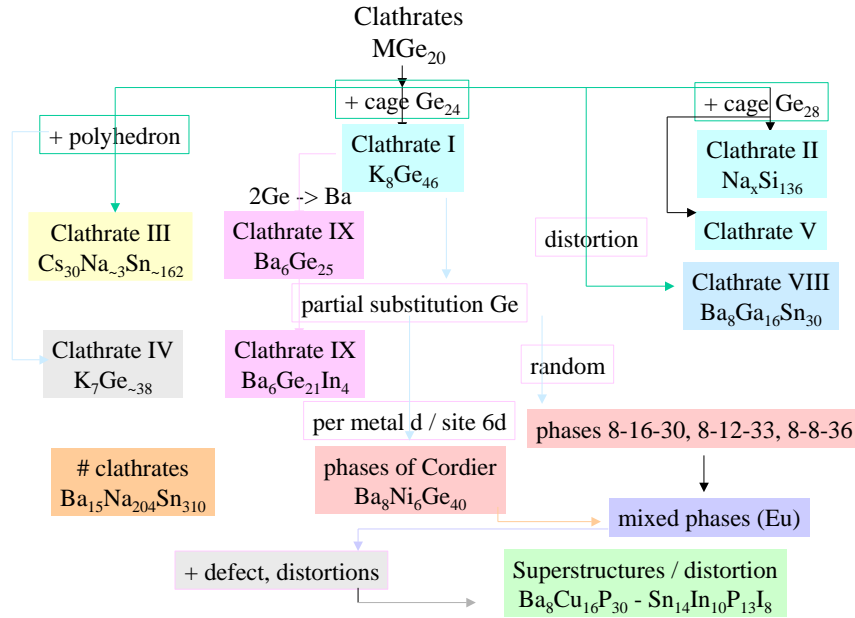


Fig. 6.9. Clathrates filiations.

Other iso-electronic substitutions (Al, In) [Mudryk 2002], [Blaque 2001] lead to semiconducting materials. Another possibility is to play on stoichiometry, for instance: $Eu_8Ga_{16+\sim x}Ge_{30-\sim x}$ [Grin 2003] or to compensate non iso-electronic substitution by vacancies in $Ba_8Zn_xGe_{46-x-y}[]_y$, with $[]$ a vacancy [Deng 2007]. Presently, only Eu- and Ba- based clathrates have lead to good ZT values in these materials, in which the control of the stoichiometry is critical, not only for TE properties but also for the appearance of parasitic phases.

The chemistry of these phases is very rich (Fig. 6.9, simplified version of [Mudryk 2002]), the studies of their physical properties should lead to new interesting compounds for TE properties.

6.2.c Penta- Hexa- tellurides

Three series of penta-tellurides and one hexa-telluride have been examined for TE properties.

In Tl_2MTe_5 ($M=Ge, Sn$), one Tl site (Tl_1) does not have close nearest neighbors whereas the (Tl_2) site has (Fig. 6.10).

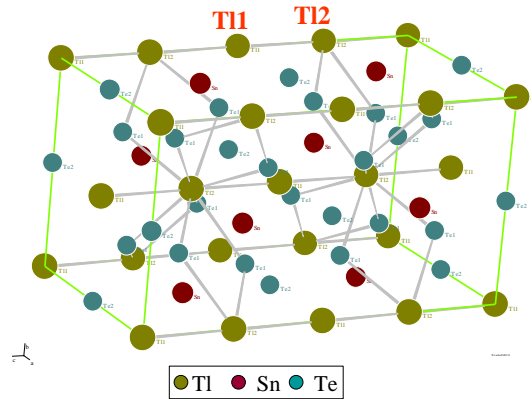


Fig. 6.10. Structure of Tl_2SnTe_5 and neighboring of Tl in site 2 and 1.

Consequently, the ADP of Tl1 are larger than that of Tl in site 2. ZT values of ~ 0.6 have been obtained [Sharp 1999]. No solid solutions have been checked until now.

The second system Re_2Te_5 ($\text{Re}_6\text{Te}_{15}$) has a complex structure (space group Pbca), with 84 atoms/unit cell and has some similitude with Chevrel's phases (octahedral clusters Re_6 and large empty cages). n- and p- type are possible by appropriate doping. The last penta-telluride Ag_9TlTe_5 has a complex structure. The thermal conductivity of this material is smaller than that of other good TE materials like Bi_2Te_3 or TAGS [Kurosaki 2005]. Ag_9TlTe_5 has a ZT of 1.2 at 700K. The hexa-telluride Tl_9BiTe_6 has also a very weak thermal conductivity and a ZT of 1.2 at 500K, a temperature where Bi_2Te_3 -based materials don't work [Wolfig 2001]. The potential of these materials is interesting from academic point of view but environmental constraints will prevent their use in devices.

6.2.d Phases with Mo clusters

The structure of Chevrel's phases is built from a three-dimensional network of pseudo-cubic clusters (Fig. 6.11) Mo_6X_8 ($\text{X} = \text{S}, \text{Se}, \text{Te}$) and its versatility authorizes the formation of various representatives.

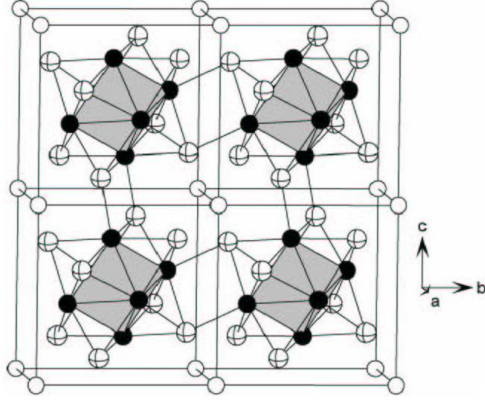


Fig. 6.11. Structure of Mo_6X_8 (Mo: ●, X: ○, empty sites ○ can be filled by Pb, Cu, ..)

The clusters form cavities or channels which can be intercalated by various elements in such a way that it is possible to modify them from metallic in Mo_6X_8 to semiconductor for a Valence Electron Concentration (VEC) of 24. Under these conditions, interesting TE properties can be expected and a ZT of 0.6 (at the high temperature of 1150K) has been found in $\text{Cu}_{3.1}\text{Mo}_6\text{Se}_8$ by studying the series $\text{M}_x\text{Mo}_6\text{Se}_8$ (M= Cu, Cu/Fe, Ti) [Caillat 1999]. Other compounds of these series have high power factors, like $\text{Ti}_{0.3}\text{Mo}_5\text{RuSe}_8$ [McGuire 2006] or $(\text{Cu}_y\text{Mo}_6\text{Se}_8)_{1-x}(\text{Mo}_4\text{Ru}_2\text{Se}_8)_x$ [Schmidt 2007]. This shows the potential of these series, specially with the possibility to replace Mo by Ru, Rh, Re to find good TE materials, of n- and p- type, stable at high temperatures ($\sim 1200\text{K}$).

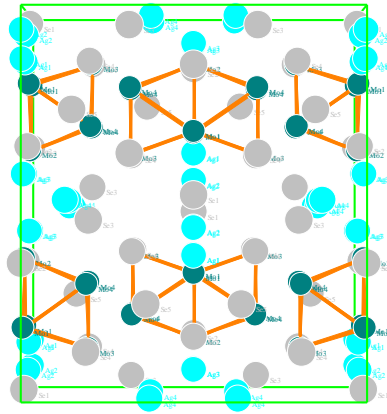


Fig. 6.12. Structure of $\text{Ag}_{3.6}\text{Mo}_9\text{Se}_{11}$ (● Mo, ● Se, ● Ag), — Mo clusters

In the phase with $\text{Mo}_9\text{Se}_{11}$ clusters, the structure owns tunnel, and the insertion of atoms (Ag, Cs, Cl) in cages [Gougeon 2004](Fig. 6.12) lead to semiconducting or semi-metallic compounds, depending on the number of electrons per clusters. These characteristics should be favorable for TE properties, which have yet not been studied in details.

However, a Seebeck coefficient of $72\mu\text{V/K}$ and a weak resistivity have been reported in $\text{Ag}_{3.6}\text{Mo}_9\text{Se}_{11}$ [Potel 2008].

Many other structural families may have empty cages in which the insertion of atoms with various oxidation degrees may lead to a semiconducting state, a prerequisite for good TE properties.

6.3. Phases with vacancies

6.3.a. Half Heusler

The cubic structure of the Heusler phases X_2YZ (space group $\text{Fm}\bar{3}\text{m}$) consists in 4 interpenetrated face centered cubic lattices in $\text{A}(0,0,0)$; $\text{B}(\frac{1}{4},\frac{1}{4},\frac{1}{4})$, $\text{C}(\frac{1}{2},\frac{1}{2},\frac{1}{2})$, et $\text{D}(\frac{3}{4},\frac{3}{4},\frac{3}{4})$, with one occupancy of the sites $\text{A}=\text{Y}$; $\text{B} \& \text{D}=\text{X}$ and $\text{C}=\text{Z}$. If one of the equivalent sites $(\frac{1}{4},\frac{1}{4},\frac{1}{4})$ or $(\frac{3}{4},\frac{3}{4},\frac{3}{4})$ is empty the Half Heusler phase ($\text{F}\bar{4}3\text{m}$) forms (Fig. 6.13).

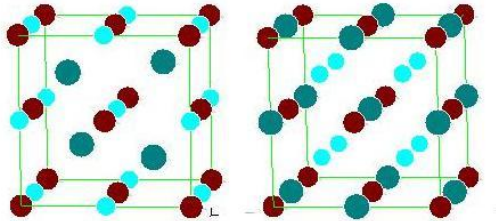


Fig. 6.13. Structures of the Heusler phases of Zr, Ni, Sn: half Heusler on left, Heusler on right (● Sn, ● Zr, ● Ni).

Among these compounds, those with 18 valence electrons have a band structure of semiconductor and often high Seebeck coefficients.

To decrease the thermal conductivity, complex substitutions with increased phonons diffusion by mass fluctuations, have been used with success (Fig. 6.14).

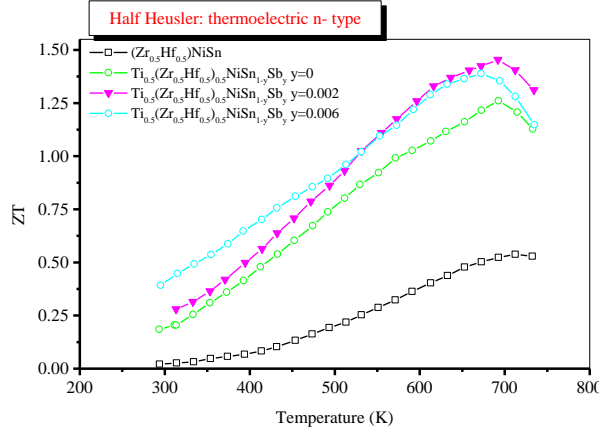


Fig. 6.14. Effect of substitutions in the half Heusler ZrNiSn

For instance, from TiNiSn ($ZT=0.4$ at 750K) and ZrNiSn, the n-type compound $\text{Hf}_{0.5}\text{Zr}_{0.5}\text{Ni}_{0.8}\text{Pd}_{0.2}\text{Sn}_{0.99}\text{Sb}_{0.01}$ has maximum of ZT of 0.7 at 800K and the n-type compound $\text{Ti}_{0.5}(\text{Zr}_{0.5}\text{Hf}_{0.5})\text{NiSn}_{0.98}\text{Sb}_{0.02}$ has a $ZT>1.4$ at 700K [Shutoh 2003]. Other systems like VFeSb ($ZT=0.11$ at 900K) have been intensively studied [Jodin 2004], but other substitutions should be examined, as simple substitutions like $\text{V}_{0.95}\text{Ti}_{0.05}\text{FeSb}$ lead to a ZT (p-type) of 0.4 at 600K. In these series, LnPdSb- type compounds (Ln= Sr, Y, rare earths, specially Er) have high Seebeck coefficients below 300K [Mastronardi 1999], [Oestreich 2003], which could lead to interesting substituted materials for cooling.

6.3.b. Zn_4Sb_3

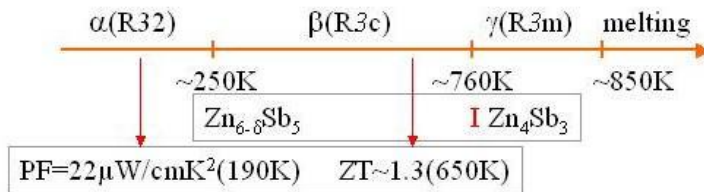


Fig. 6.15. Scheme of structural and Te properties of Zn_4Sb_3 .

Zn_4Sb_3 exists under three crystallographic varieties: α -phase stable below -10°C , β -phase from -10°C to 492°C and γ -phase from 492°C to the melting temperature of 566°C . The structural and TE properties are summarized in Fig. 6.15.

The β -phase leads to TE materials (p-type), with a high ZT of 1.3 at $\sim 650\text{K}$ [Caillat 1997], further increased to 1.4 at 525K by substitution in $\text{Zn}_{3.2}\text{Cd}_{0.8}\text{Sb}_3$ [Caillat 1999a].

In Zn_4Sb_3 the observation of vacancies, Zn-interstitials and of 2 types of Sb atoms (spherical ion Sb^{3-} and dimers Sb^{4-}) (Fig. 6.16) induce a strong disorder [Snyder 2004] (in fact the composition is $\sim \text{Zn}_{6-w}\text{Sb}_5$) which contribute to the decrease of the thermal conductivity.

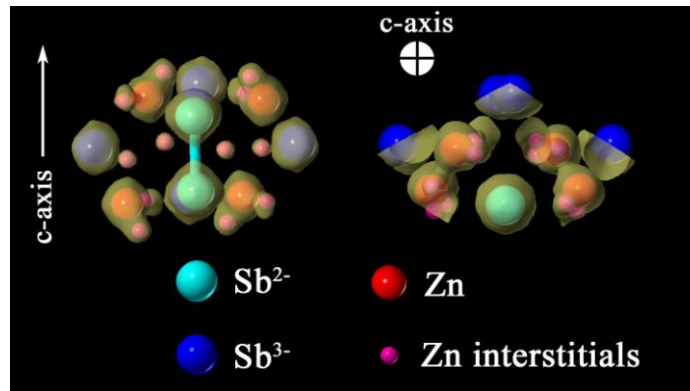


Fig. 6.16. Disorder in the structure of Zn_4Sb_3 .

A phonon mode of low energy has been associated to Sb dimers [Schweika 2007]. It does not seem that doping lead to achieving the n-type.

6.4. Complex solid solutions derived from conventional materials

6.4.a. Bi_2Te_3 - derivatives

As Bi_2Te_3 is the archetype of TE materials used for cooling applications, few derivatives systems have been studied.

At low temperature, TE properties of CsBi_4Te_6 doped by 0.05% SnI_3 are equivalent to old $\text{Bi}_{2-x}\text{Sb}_x\text{Te}_{3-y}\text{Se}_y$ compositions with a $\text{ZT} \sim 0.8$ at 225K, of possible use for cooling [Chung 2000].

Strongly doped single crystals lead to higher values than $\text{ZT} \sim 0.8-0.9$ at $\sim 300\text{K}$. The best values concern n-type $(\text{Bi}_{0.25}\text{Sb}_{0.75})_2\text{Te}_3$ doped with 0,07% I (in mass), 0,02% Te, et 0,03% CuBr [Yamashita 2004] leading to a $\text{ZT} > 1,1$ at $\sim 300\text{K}$. For the p-type, doping by 8% in mass of Te leads to $\text{ZT} = 1.4$ at the same temperatures [Yamashita 2003]. The effects of Te doping as well as those of texturation induced by extrusion were previously studied in $\text{Bi}_{0.5}\text{Sb}_{1.5}\text{Te}_3$ [Hong 2003]. On the con-

trary, the addition of few percents of PbTe in $\text{Bi}_{0.4}\text{Sb}_{1.6}\text{Te}_3$ do not lead to an improvement of ZT.

$\text{K}_2\text{Bi}_8\text{Se}_{13}$ forms two phases : $\alpha\text{-K}_2\text{Bi}_8\text{Se}_{13}$ (triclinic, space group $P\bar{1}d$) et $\beta\text{-K}_2\text{Bi}_8\text{Se}_{13}$ (monoclinic, space group $P2_1/m$). The β -phase (Fig. 6.17) has an architecture built from fragments structure type of Bi_2Te_3 , CdI_2 and NaCl , and a mixed occupancy of the sites K/Bi [Bilc 2005].

In $\text{K}_2\text{Bi}_8\text{Se}_9\text{S}_4$, all the S sites are with a mixed occupancy and the representation (Fig. 6.17) is made according to the nature of the main occupant of the site. The thermal conductivity is very weak (complex structure, atoms vibrating in tunnels, disorder in the site occupancy) and the doping increases the Seebeck coefficient, however the ZT values are presently too small for cooling applications. Other substitutions could possibly lead to p-type materials.

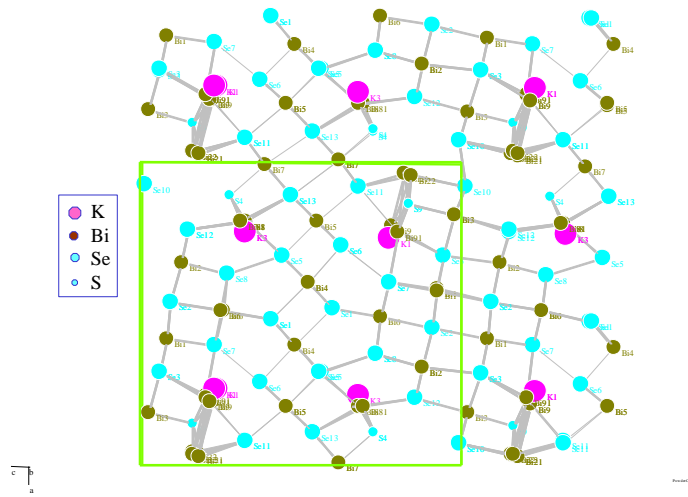


Fig. 6.17. Structure of $\text{K}_2\text{Bi}_8\text{Se}_9\text{S}_4$

6.4.b derivatives from PbTe and TAGS

The series of cubic materials $\text{AgPb}_m\text{SbTe}_{2+m}$ (space group $\text{Fm}\bar{3}m$) (Fig. 6.18) has lead to type n semiconductor with high ZT values when $m=10$ ($\text{ZT}=1$ at 700K) or $m=18$ ($\text{ZT}=2.2$ at 800K) [Hsu 2004].

Smallest values of ZT have been observed in annealed Ag-deficient samples ($\text{ZT}=1.1$ at 670K with $x=0.4$ and $\text{ZT}=0.3$ with $x=0.3$). However these materials are not conventional bulk but composites (see below $\text{In}_2\text{O}_3 + \text{Ge}$).

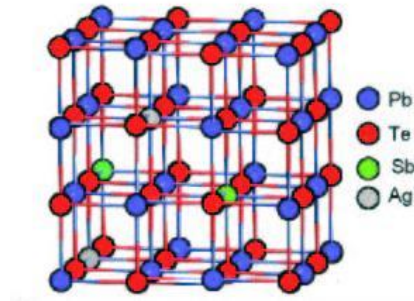


Fig. 6.18. Cubic structure of $\text{AgPb}_m\text{SbTe}_{2+m}$

High resolution transmission microscopy have shown that Ag-Sb rich phase nano-crystals exist in a Pb-Te rich matrix, that has also been described as nano-clusters of $\text{AgPb}_3\text{SbTe}_5$ in PbTe matrix [Lin 2005]. Such nano-phases could be responsible of high ZT values, theoretically predicted, and observed in quantum wells super-lattice, nano-dots etc.. (see below nano-materials). The difficult control of the nature, size and dispersion of these nano-phases could be responsible of the mismatch of literature results. The effect of annealing and of eventual temperature cycling which could induce a growth of these nano-objects have not yet been checked.

6.5. Other intermetallic compounds

Recently, few new Sb-based compounds have been identified with good TE characteristics, a property which can be due to the property of Sb to diffuse phonons more efficiently than lighter ions with the same electronic configuration (we already mention that for skutterudites and for Zn_4Sb_3). Moreover, materials made from metalloid and slightly more electropositive elements (Zintl phase) seems to be able to have high ZT.

6.5.1 $\text{Yb}_{14}\text{MnSb}_{11}$

The tetragonal structure of $\text{Yb}_{14}\text{MnSb}_{11}$ (space group $I4_1/acd$) is complex (Fig. 6.19) and built from various structural units. The flexibility to accommodate various elements (possibility of future improvements?) have lead to a $\text{ZT}=1$ at the high temperature of 1220K in this p-type material [Brown 2006].

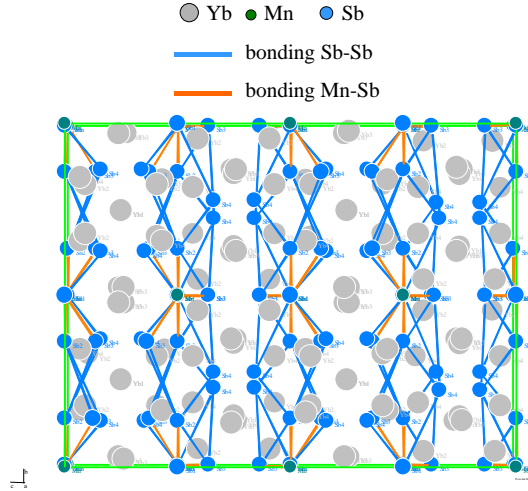


Fig. 6.19. (100) projection of the structure of $\text{Yb}_{14}\text{MnSb}_{11}$

6.5.2. $\text{Mo}_3\text{Sb}_{7-x}\text{Te}_x$ and derivatives

The structure Ir_3Ge_7 (space group $\text{Im}\bar{3}\text{m}$) of $\text{Nb}_3\text{Te}_{7-x}\text{Sb}_x$ [Wang 2002] and of $\text{Mo}_3\text{Sb}_{7-x}\text{Te}_x$ ($x=1,5$ et $1,6$) [Gascoin 2007] compounds forms infinite chains in the three directions of space. $\text{Mo}_3\text{Sb}_{7-x}\text{Te}_x$ only exists for a VEC between 51 and 56, a value of 55 being a prerequisite to obtain a semiconductor.

With a ZT of 0.8 in $\text{Mo}_3\text{Sb}_{5,4}\text{Te}_{1,6}$ at 1050K [Gascoin 2007] and in $\text{Mo}_{3-y-z}\text{Ru}_y\text{Fe}_z\text{Sb}_7$ at 1000K [Candolfi 2008] for $(y,z) = (0.16,0.5)$ and $(0.1,0.7)$ these materials are better than the best p-type Si-Ge.

6.5.3. Other Sb-based materials

A ZT of 0.55 at 600K was initially attributed to the phase Mg_3Sb_2 (space group $\text{P}\bar{3}\text{m}1$) which was invalidated with a maximum of ZT of 0.2 at 875K [Condon 2006]. Moreover, the phase loses Mg and oxidizes above 900K.

The structure of CaZn_2Sb_2 is the same than that of Mg_3Sb_2 and the material easily oxidizes. Due to its simple crystalline structure, its TE properties are poor with a ZT of 0.5 at 770K [Stark 2002].

6.5.4. $\text{Mg}_2\text{Si}_{1-x}\text{Sn}_x$

During the years 1960, the Ioffé Institute showed that the compounds Mg_2X ($\text{X}=\text{Si}$, Ge or Sn) are semiconductors with a band structure which should favor TE properties. Various substitutions have been tested and the best results have been obtained when the mass difference between elements is the highest, i.e., with Si and Sn [Fedorov 2003]. A ZT of 1.1 has then been found at 800K, a better value than with n-type Si-Ge [Zaitsev 2006].

6.6. Oxides

The main expected advantage of oxides is their chemical stability in oxidizing atmosphere, even though the stability and transport properties of some oxides depend on the partial pressure of oxygen. If many oxides have high Seebeck coefficients ($\alpha > 100 \mu\text{V/K}$) their performance are presently limited by electrical resistivities much higher than in previously described materials.

6.6.1. Cobaltites

Among the most promising p-type oxides, cobaltites with conductive layers of CoO_2 (CdI_2 type) have been the starting point of interest for TE oxides with Na_xCoO_2 : a metallic oxide with a high Seebeck coefficient [Terasaki 1997].

6.6.2. misfit oxides

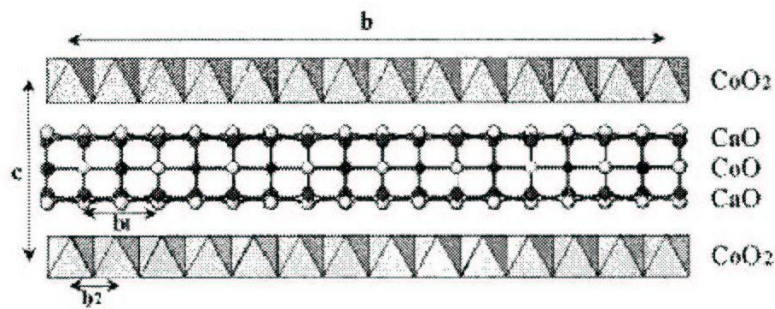


Fig. 6.20. Structure of the misfit compound $\text{Ca}_3\text{Co}_4\text{O}_9$ ($b \sim 8b_1 \sim 13b_2$)

Among cobaltites, the layered compound $\text{Ca}_3\text{Co}_4\text{O}_9$ is in fact a lamellar oxide with misfit structure [Masset 2000] of general formulae: $[\text{AO}]_n[\text{RS}[\text{CoO}_2]_{b_1/b_2}]$ made of CoO_2 planes (as in Na_xCoO_2) split by AO layers of NaCl type (RS: rock salt) with

possible n values of 2, 3 and 4. Considering the sub-lattice CoO_2 as a mono-layer NaCl (quoted S_2) which matches with the sub-lattice AO (S_1) along the a -axis but mismatches along b -axis. The ratio of b -axis of S_1 and S_2 , i.e., b_1/b_2 measures the incommensurability of the two lattices (Fig. 6.20). In the case of $\text{Ca}_3\text{Co}_4\text{O}_9$, this ratio is 1.625 (13/8) which leads to a formulae: $[\text{Ca}_2\text{CoO}_3]_{\text{RS}}[\text{CoO}_2]_{1.62}$.

The family of lamellar oxides with misfit structure is very large (choice on n , and A , for instance Ca , Bi , Sr ,... and replacement of Co by Rh , ...) and many new materials are conceivable, however the actual ZT values are low due to high electrical resistivity [Koumoto 2006].

The highest ZT value in an oxide has been obtained in a small size single crystal of Na_xCoO_2 (estimated value of 1.2 at 800K). The impossibility to grow large enough single crystal for applications has lead to many studies concerned by texturation processes, with the drawback that the electrical conductivity in the CoO_2 planes decrease as compared to crystals.

6.6.3. other oxides

Other oxides families have also been studied like perovskites ACoO_3 -type, manganites AMnO_3 [Kuwahara 2004], delafossites CuMO_2 [Ono 2006], YBCO ($\text{YBa}_2\text{Cu}_3\text{O}_{6+y}$), ZnO [Tanaka 1997] [Orikasa 2008], ruthenates ARuO_3 [Hébert 2001] and A_2RuO_4 , In_2O_3 etc.. The best ZT values reach 0.4 for the p -type and 0.3 for the n -type in conventional oxides and of 0.55 in misfits oxides.

The structure of In_2O_3 (space group $1a-3$) shows alternatively ordered and disordered In -planes (see Fig. 6.21)

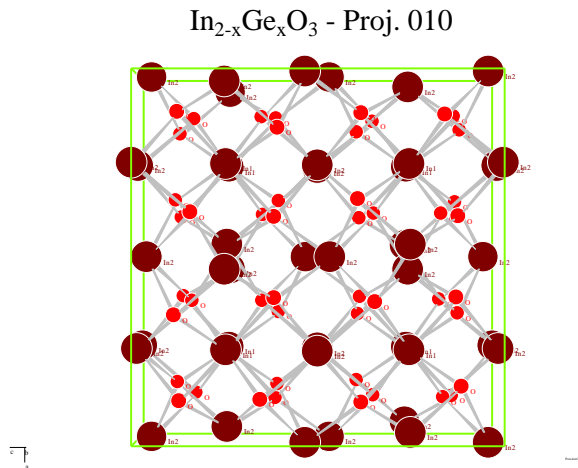


Fig. 6.21. (010) projection of In_2O_3 structure

The solubility limit of Ge is no more than 0.5 atom%, for higher rate of Ge the material forms a composite In_2O_3 + inclusions of micronic size ($\sim 100\mu\text{m}$) of $\text{In}_2\text{Ge}_2\text{O}_7$. In that composite, the thermal conductivity is notably reduced and a ZT of 0.45 at 1243K has been observed which is actually the best value for a n-type oxide.

This shows the potential of micro-composites, as well as nano-composites (see $\text{Ag}_{1-x}\text{Pb}_{18}\text{SbTe}_{20}$), to improve ZT values as compared to "parent" materials.

6.7: ZT of new materials

The use of the various processes, previously described, to minimize the thermal conductivity has lead to a noticeable increase of ZT from ~ 1995 . Let us remark that the new families of materials have lead to the improvement of ZT, moreover, they have increased the temperature ranges where the TE can be used. The value of ZT in few families is higher than 1.3 (30% increase as compared to conventional materials). The best value in a bulk material is actually of 1.7 in skutterudites. The curves of the best values of ZT versus temperature in bulk materials are shown in Fig. 6.22 and 6.23 for the p- and n-type materials, respectively.

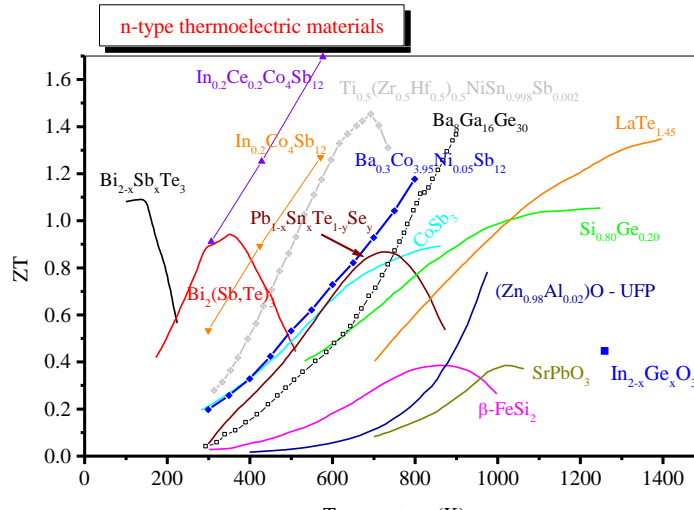


Fig. 6.22. Best ZT values for representatives of n-type materials

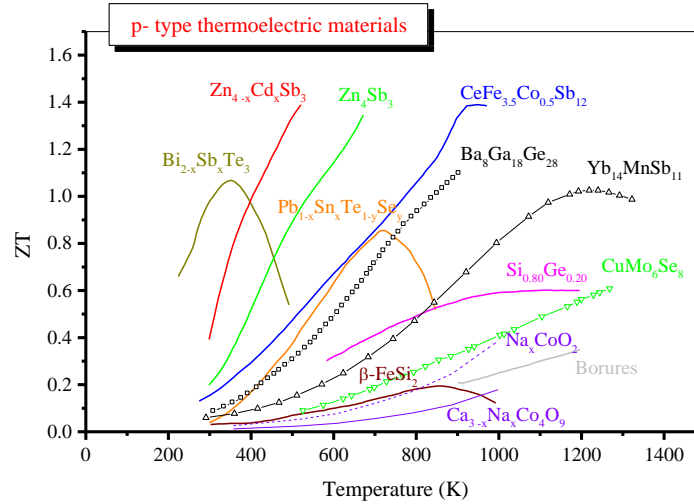


Fig. 6.23. Best ZT values for representatives of p-type materials

6.8. Semiconducting glasses

A certain number of characteristics leading to a weak thermal conductivity and to good TE properties, such as complex structures, inclusions, impurities, mass fluctuations, disorder, ... can be found in glass. However, glass is generally insulator except the metallic glasses which have low Seebeck coefficients (as metals). Numerous semiconducting glasses, with a small gap to favor high Seebeck coefficients, exist specially in pnictides and chalcogenides. Their preliminary studies have shown encouraging results, even though the electrical resistivity is generally too high [Gonçalves et al., in this volume] .

7. Nano TE materials

Transport properties in micro-, and nano- structures differ from that in bulk 3D (three-dimensional) materials. The thermal conductivity of nano-structures like super-lattices (material with periodic change of nano-metric layers of various elements or substances) is weaker than in bulk materials. This is a positive aspect for TE properties. However, these nano-structures are generally obtained by thin films techniques (Molecular Beam Epitaxy, Knudsen cells, Pulsed laser, CVD, ..) too costly to be used for the production of materials for large scale applications. Moreover, their weak thickness are not very compatible with the formation of

large temperature gradients. Conversely, they are well adapted to micro-cooling in electronics.

Electronic transport properties are also strongly modified by dimensionality effects on the band structure (Fig. 7.1) [Dresselhaus 1999].

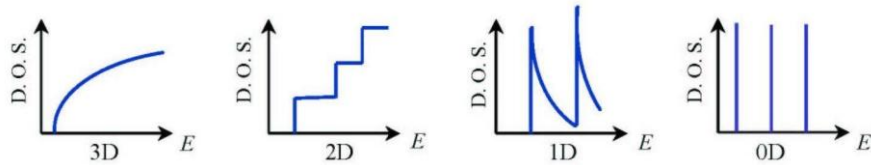


Fig. 7.1. DOS for a semiconductor 3D, a quantum well 2D, a nano-wire or nano-tube 1D and a quantum dot 0D

To summarize, in a 3D material, α , σ and λ are bound and it is difficult to optimize both of them, in the case of lower dimension new possibilities exist to independently adjust them.

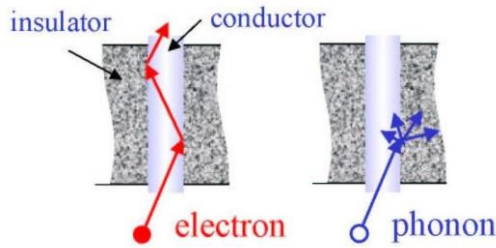


Fig. 7.2.. Proposed model for the diffusion of phonons and carriers in a 1D structure

In addition, new interfaces are created which can increase the phonon diffusion, more than that of carriers, leading to an increase value of ZT (Fig. 7.2)

It is remarkable that the improvement of ZT has been theoretically predicted [Hicks 1993] (Fig. 7.3) before its experimental observation.

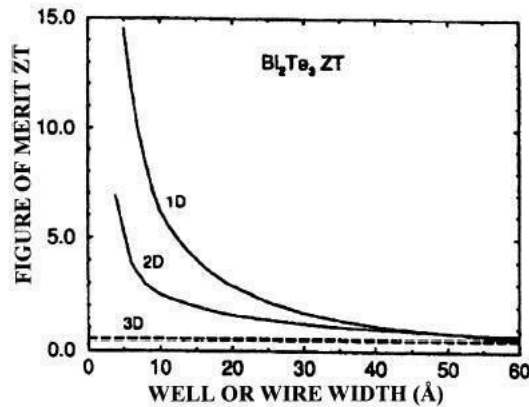


Fig. 7.3. Evolution of ZT with the dimensionality

The experimental proofs, in various forms of nano-structures, concern, for instance:

- super lattices including quantum wells PbTe-PbSeTe [Hicks 1996], in which ZT value of 1.6 has been calculated (in front of 0.4 for the bulk)
- super lattices of $\text{Bi}_2\text{Te}_3/\text{Sb}_2\text{Te}_3$, with a ZT of 2.4 (in front of 1.0 for the bulk) [Venkatasubramanian 2001]
- a decrease of the thermal conductivity of a Ge matrix by inclusions of Si-nano-wires which depends on the diameter of the nano-wires [Yang 2005]
- an increase of the ZT value in various compositions of Bi_2Te_3 by addition of Bi_2Te_3 -nano-powders [Ni 2005]...

These two last examples, as well as the case of $\text{AgPb}_m\text{SbTe}_{2+m}$ (see above) show that the study of nano-composites may allow to benefit of TE performances related to the nano-sizes with samples of large sizes (> centimeter) requested for applications. The next year should be crucial for the understanding of mechanisms in nano-composites and consequently to be able to increase beneficial effects of such systems as compared to detrimental effects, for instance, on resistivity.

8. Shaping of nano-composites TE materials

The shaping of such samples can be realized by hot pressing techniques. In the recent studies, this shaping is generally obtained by Spark Plasma Sintering (SPS) technique, a technique of fast sintering under pressure, which mainly avoid grain growth observed with conventional hot press. A small size SPS machine, as we acquired in CNRS Thiais (Syntex 515S), is able to perform sintering under conditions up to 50MPa and 2000°C, with non costly graphite crucibles. Sample diameters of up to 20-25 mm are obtained for sintering temperature up to ~1500°C for

ceramics and $\sim 1000^\circ\text{C}$ for intermetallics; for higher temperatures smaller diameter can be produced. These temperatures are generally sufficient as the pressure helps to sinter. Pressures of up to 500MPa have been realized with other crucibles (W-C) at lower temperatures and diameter.

Such techniques has been used with various TE conventional powders (grains smaller than a few $10\mu\text{m}$) of Bi_2Te_3 , skutterudites, clathrates, half Heusler, Zn_4Sb_3 , $\text{Mg}_2(\text{Si},\text{Sn})$, PbTe , ZnO derivatives, etc.. Electric contact or protection against corrosion can be made, in few cases, by direct sintering of a thin metal foil with the powder.

More recently, the technique has been successfully applied in various composites systems, the starting nano-particles being produced by sol-gel method, electro-chemistry,... but more often from ball milling:

- various compositions of Bi_2Te_3 with addition of Bi_2Te_3 -nano-powders [Ni 2005]
- synthesis of $\text{Yb}_y\text{Co}_4\text{Sb}_{12}/\text{Yb}_2\text{O}_3$ composites [Zhao 2006]
- shaping of composite made of nano-particles of SiC dispersed in Bi_2Te_3 [Zhao 2008]
- shaping of binary skutterudites with C_{60} inclusions [Shi 2004]
- mixing of micro-nano- skutterudites [Zhang 2006]
- Bi addition in Heusler V_2FeAl [Mikami 2008]
- nano-inclusions of ZrO_2 in the half Heusler $\text{Zr}_{0.5}\text{Hf}_{0.5}\text{Ni}_{0.8}\text{Pd}_{0.2}\text{Sn}_{0.99}\text{Sb}_{0.01}$ [Chen 2006]

It is remarkable that such sintering process takes place within a short period of time (typically few minutes) and lead to density higher than 95% of the theoretical X-ray density, a very crucial parameter for TE transport properties. This explains the increasing used of this technique for the synthesis and/or shaping of TE materials and micro-, nano-composites from 2004.

As a conclusion, within the 15 last years, bulk materials with an increased complexity (structure, solid solutions) have lead to an improvement of the TE figure of merit of $\sim 30\%$, and sometime more, in various series. Complexity of the micro-, nano-structure seems actually promising to overtake the actual ZT values. Studies of nano-composites coupled by fast shaping process by SPS, should lead to a real potential of using thermoelectricity for large scale applications.

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